

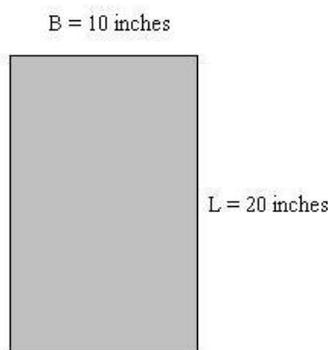
## Strength of Materials Math Worksheet **Answers**

1. Calculate the maximum tensile and compressive forces allowed for the cross-sectional area shown in Figure 1. The maximum tensile strength is  $500 \text{ lb/in}^2$  (pounds per inches squared). The maximum compressive strength is  $5,000 \text{ lb/in}^2$ . Use the following equations to complete the problem. Show your work and calculations.

cross-sectional area = (B) x (L)

maximum tensile force = (maximum tensile strength) x (cross-sectional area)

maximum compressive force = (maximum compressive strength) x (cross-sectional area)



**Answer:**

Cross-sectional area = (10 inches) x (20 inches) =  $200 \text{ in}^2$

Maximum tensile force =  $(500 \text{ lb/in}^2) \times (200 \text{ in}^2) = 100,000 \text{ lb}$

Maximum compressive force =  $(5,000 \text{ lb/in}^2) \times (200 \text{ in}^2) = 1,000,000 \text{ lbs}$

Figure 1: Cross-sectional area.

2. Calculate the maximum tensile and compressive forces allowed for the following two cross-sectional areas shown in Figure 2. The maximum tensile strength is  $3,750 \text{ lb/in}^2$ . The maximum compressive strength is  $4,850 \text{ lb/in}^2$ . Use the following equations along with those in #2 to complete the problem. Show your work and calculations.

cross-sectional area =  $\pi \times (\text{radius})^2$

$\pi = 3.14$

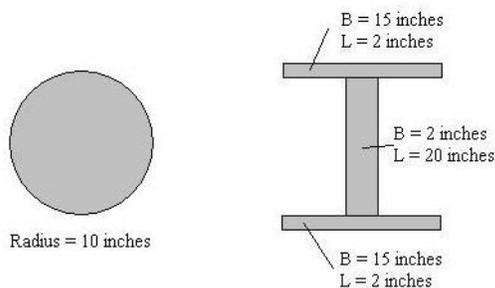


Figure 2: Cross-sectional areas.

**Answer:**

Cross-sectional area of circle =  $3.14 \times (10 \text{ in})^2 = 314 \text{ in}^2$

Cross-sectional area of I-beam = (15 inches) x (2 inches) + (15 inches) x (2 inches) + (2 inches) x (20 inches) =  $100 \text{ in}^2$

Maximum tensile force of circle =  $(3,750 \text{ lb/in}^2) \times (314 \text{ in}^2) = 1,177,500 \text{ lb}$

Maximum compressive force of circle =  $(4,850 \text{ lb/in}^2) \times (314 \text{ in}^2) = 1,522,900 \text{ lb}$

Maximum tensile force of I-beam =  $(3,750 \text{ lb/in}^2) \times (100 \text{ in}^2) = 375,000 \text{ lb}$

Maximum compressive force of I-beam =  $(4,850 \text{ lb/in}^2) \times (100 \text{ in}^2) = 485,000 \text{ lb}$

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3. Part 1: Calculate the compressive force for the cross-sectional area shown in Figure 3. The original length of the member was 100-in long. After applying the compressive force, the member was 99-in long. The modulus of elasticity for the material used in the cross section is 10,000 lb/in<sup>2</sup>. Use the following equations along with those in #2 and #3 to complete the problem. Show your work and calculations.

Part 2: Calculate the tension force for the cross-sectional area shown in Figure 3. The original length of the member was 100-in long. After applying the tensile force, the member was 103-in long. The modulus of elasticity for the material used in the cross section is the same as in #2 above. Use the following equations along with those in #2 and #3 to complete the problem. Show your work and calculations.

$$\sigma = E * \epsilon$$

$$\epsilon = \text{change in length} / \text{original length}$$

E = modulus of elasticity

$$\text{change in length} = (\text{length after force applied}) - (\text{original length})$$

If the change in length is negative, take the absolute value to get a positive number

$$\text{force} = \sigma * \text{cross-sectional area}$$

$\sigma$  = stress

$\epsilon$  = strain

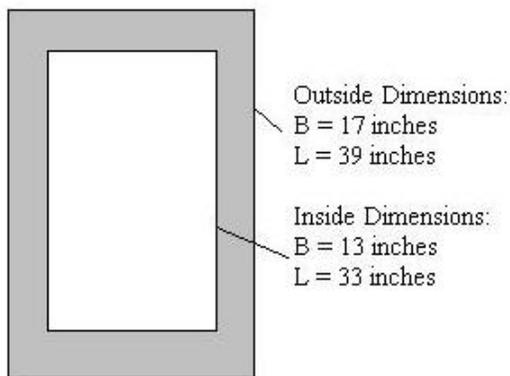


Figure 3: Cross-sectional area.

**Part 1 Answer:**

$$\text{Change in length} = 99 \text{ inches} - 100 \text{ inches} = -1 \text{ inch}$$

$$\text{Taking the absolute value, change in length} = 1 \text{ inch}$$

$$\epsilon = 1 \text{ inch} / 100 \text{ inches} = 0.01$$

$$\sigma = (10,000 \text{ lb/in}^2) \times (0.01) = 100 \text{ lb/in}^2$$

$$\text{Cross-sectional area} = (17 \text{ inches}) \times (39 \text{ inches}) - (13 \text{ inches}) \times (33 \text{ inches}) = 234 \text{ in}^2$$

$$\text{Force} = (100 \text{ lb/in}^2) \times (234 \text{ in}^2) = 23,400 \text{ lb}$$

**Part 2 Answer:**

$$\text{Change in length} = 103 - 100 \text{ inches} = 3 \text{ inches}$$

$$\epsilon = 3 \text{ inches} / 100 \text{ inches} = 0.03$$

$$\sigma = (10,000 \text{ lb/in}^2) \times (0.03) = 300 \text{ lb/in}^2$$

$$\text{Cross-sectional area} = (17 \text{ inches}) \times (39 \text{ inches}) - (13 \text{ inches}) \times (33 \text{ inches}) = 234 \text{ in}^2$$

$$\text{Force} = (300 \text{ lb/in}^2) \times (234 \text{ in}^2) = 70,200 \text{ lb}$$