

## Lesson Problem Statement **Answer Key**

**Lesson problem statement:** Your objective is to place some pencils in a tray such that they are stable. This means that you must align the long axes of the pencils with the groove in the tray. You know that a golf pencil (x) is 3.5-inches long and a regular pencil (y) is 7.5-inches long. The tray has room for no more than 52.5 linear inches of pencils (the groove is 52.5 inches long). **Question:** How many of each pencil should you use in order to maximize the total number of pencils in the tray?

1. Inequalities to graph are:

$$x \geq 0$$

$$y \geq 0$$

$$y \leq -\frac{7}{15}x + 7$$

2. The corner points of the shaded region are:

$$(0,0)$$

$$(15,0)$$

$$(0,7)$$

3. The optimization equation is:

$$z = x + y$$

4. The values of the optimization equation at each corner point are:

$$z(0,0) = 0 + 0 = 0$$

$$z(15,0) = 15 + 0 = 15$$

$$z(0,7) = 0 + 7 = 7$$

5. The maximum value is:

$$z(15,0) = 15$$

6. The final solution is:

**15 golf pencils and 0 regular pencils**