

Name: \_\_\_\_\_ Key \_\_\_\_\_ Date: \_\_\_\_\_ Class/Period: \_\_\_\_\_

### Linear Regression Activity

The table below shows the number of small specimen-BMD scanners in the United States from 1998 to 2004.

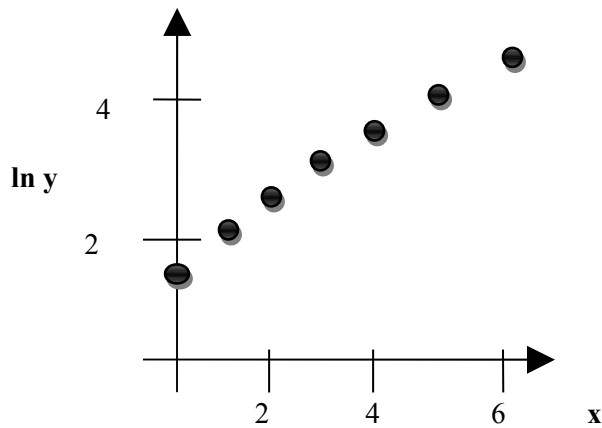
Year	1998	1999	2000	2001	2002	2003	2004
Small Specimen BMD Scanners	5	8	13	21	33	52	80

- a. **Linearize the data. That is, make a table with  $x$ - and  $y$ -values, where  $x$  is the number of years since 1998 and  $y$  is the number of BMD scanners. Then make a scatter plot of the linearized data.**

Subtract 1998 from each year (your  $x$ ) and find the natural logarithm of each BMD scanner quantity.

$x$	0	1	2	3	4	5	6
$\ln y$	1.60944	2.07944	2.56495	3.04452	3.49651	3.94124	4.38203

The scatter plot suggests that there may be a linear relationship between  $x$  and  $\ln y$ . Plot your points here and be sure to label and scale your axis.



- b. **Find a regression equation for the linearized data.**

Use **LinReg(ax+b)** on the STAT CALC screen to find the linear regression equation. **LinReg**

$$y = ax + b$$

$$a = 0.464033$$

$$b = 1.626204$$

$$r^2 = 0.99963$$

$$r = 0.99981$$

Write out linear equation:  $\ln y = 0.4640x + 1.6262$

- c. Use the linear regression equation to find an exponential model for the original data.

To find a model solve the regression equation in part **b** for  $y$ .

$$\ln y = 0.4640x + 1.6262$$

$$e^{\ln y} = e^{0.4640x + 1.6262}$$

$$y = e^{0.4640x + 1.6262}$$

$$y = e^{0.4640x} \cdot e^{1.6262}$$

$$y = 5.0845e^{0.4640x}$$

*Raise  $e$  to each side.*

$$e^{\ln y} = y$$

*Product Property of Exponents*

$$e^{1.6262} \approx 5.0845$$

The number of small-specimen BMD scanners in the United States between 1998 and 2004 can be modeled by the exponential function  $y = 5.0845e^{0.4640x}$ .

- d. Use the exponential model to predict the number of web sites that there will be in 2015.

The year 2015 is 17 years after 1998, so replace  $x$  with 17 in the exponential function.

$$y = 5.0845e^{0.4640x}$$

$$y = 5.0845e^{0.4640(17)}$$

$$y = \mathbf{13,550.74} \text{ BMD scanners in 2015.}$$

Yes, this prediction makes sense.